

## **KS1 CALCULATION POLICY**

The following pages show progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

#### **KEY STAGE 1**

Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction.

**Key language:** whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table

Addition and subtraction: Children first learn to connect addition and subtraction with counting, but they soon develop two very important skills: an understanding of parts and wholes, and an understanding of unitising 10s, to develop efficient and effective calculation strategies based on known number bonds and an increasing awareness of place value. Addition and subtraction are taught in a way that is interlinked to highlight the link between the two operations. A key idea is that children will select methods and approaches based on their number sense. For example, in Year 1, when faced with 15 - 3 and 15 - 13, they will adapt their ways of approaching the calculation appropriately. The teaching should always emphasise the importance of mathematical thinking to ensure accuracy and flexibility of approach, and the importance of using known number facts to harness their recall of bonds within 20 to support both addition and subtraction methods.

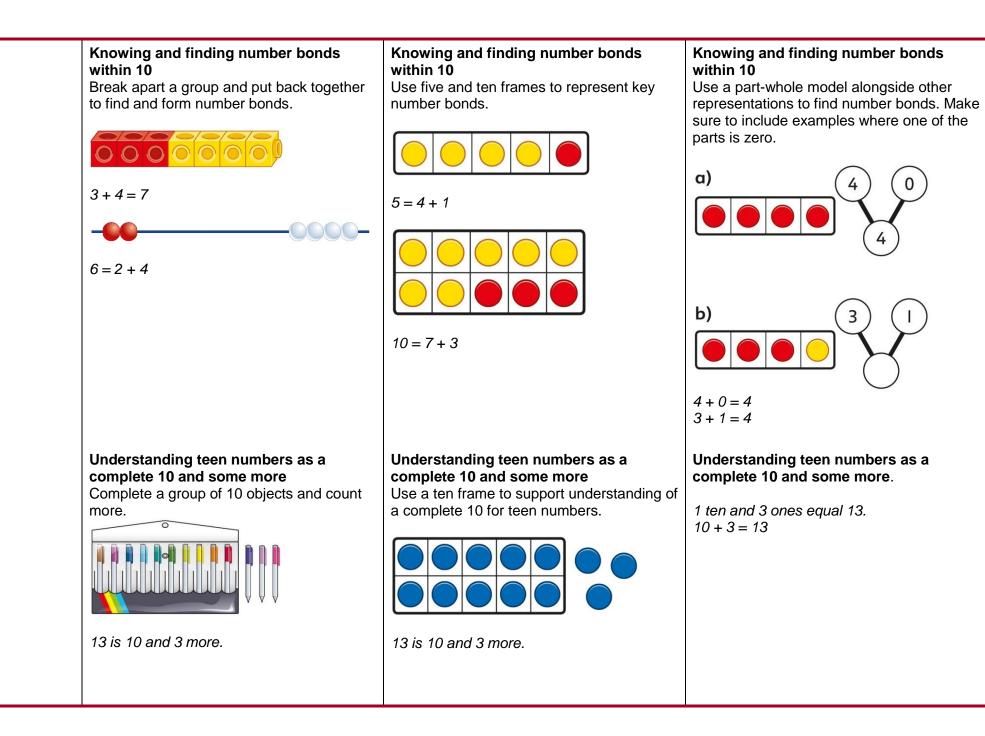
In Year 2, they will start to see calculations presented in a column format, although this is not expected to be formalised until KS2. We show the column method in Year 2 as an option; teachers may not wish to include it until Year 3. **Multiplication and division:** Children develop an awareness of equal groups and link this with counting in equal steps, starting with 2s, 5s and 10s. In Year 2, they learn to connect the language of equal groups with the mathematical symbols for multiplication and division.

They learn how multiplication and division can be related to repeated addition and repeated subtraction to find the answer to the calculation. In this key stage, it is vital that children explore and experience a variety of strong images and manipulative representations of equal groups, including concrete experiences as well as abstract calculations.

Children begin to recall some key multiplication facts, including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.

**Fractions:** In Year 1, children encounter halves and quarters, and link this with their understanding of sharing. They experience key spatial representations of these fractions, and learn to recognise examples and non-examples, based on their awareness of equal parts of a whole. In Year 2, they develop an awareness of unit fractions and experience non-unit fractions, and they learn to write them and read them in the common format of numerator and denominator.

		Year 1	
	Concrete	Pictorial	Abstract
Year 1 Addition <u>Key Vocab</u>	<b>Counting and adding more</b> Children add one more person or object to a group to find one more.	<b>Counting and adding more</b> Children add one more cube or counter to a group to represent one more.	<b>Counting and adding more</b> Use a number line to understand how to lin counting on with finding one more.
Addition Plus Total Altogether			one more 0 1 2 3 4 5 6 7 8 9 10
		One more than 4 is 5.	One more than 6 is 7. 7 is one more than 6.
			Learn to link counting on with adding more than one. 0  1  2  3  4  5  6  7  8  9  10 5 + 3 = 8
	Understanding part-part-whole relationship Sort people and objects into parts and understand the relationship with the whole.	Understanding part-part-whole relationship Children draw to represent the parts and understand the relationship with the whole.	Understanding part-part-whole relationship Use a part-whole model to represent the numbers. 10 6 $46$ $+$ $4$ $=$ $10$
	The parts are 2 and 4. The whole is 6.	The parts are 1 and 5. The whole is 6.	6 + <i>4</i> = 10



#### Adding by counting on

Children use knowledge of counting to 20 to find a total by counting on using people or objects.



#### Adding the 1s

Children use bead strings to recognise how to add the 1s to find the total efficiently.

2 + 3 = 5 12 + 3 = 15

## Bridging the 10 using number bonds

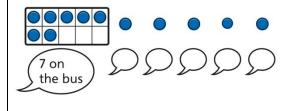
Children use a bead string to complete a 10 and understand how this relates to the addition.



7 add 3 makes 10. So, 7 add 5 is 10 and 2 more.

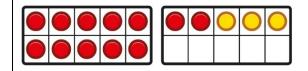
#### Adding by counting on

Children use counters to support and represent their counting on strategy.



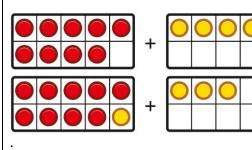
#### Adding the 1s

Children represent calculations using ten frames to add a teen and 1s.



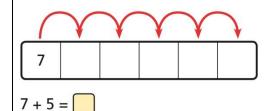
2 + 3 = 5 12 + 3 = 15

**Bridging the 10 using number bonds** Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.



#### Adding by counting on

Children use number lines or number tracks to support their counting on strategy.



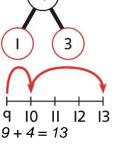
#### Adding the 1s

Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.

3 + 5 = 8 So, 13 + 5 = 18

#### Bridging the 10 using number bonds

Use a part-whole model and a number line to support the calculation.



#### Year 1 Subtraction

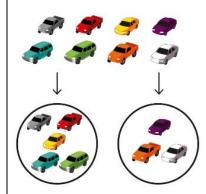
Key Vocab Subtract Subtraction Find the difference Take away Minus Less **Counting back and taking away** Children arrange objects and remove to find how many are left.



1 less than 6 is 5. 6 subtract 1 is 5.

# Finding a missing part, given a whole and a part

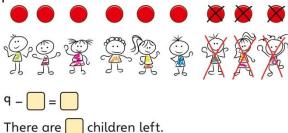
Children separate a whole into parts and understand how one part can be found by subtraction.



8 - 5 = ?

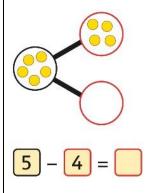
## Counting back and taking away

Children draw and cross out or use counters to represent objects from a problem.



# Finding a missing part, given a whole and a part

Children represent a whole and a part and understand how to find the missing part by subtraction.



#### Counting back and taking away

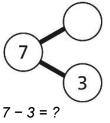
Children count back to take away and use a number line or number track to support the method.



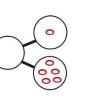
9 - 3 = 6

# Finding a missing part, given a whole and a part

Children use a part-whole model to support the subtraction to find a missing part.



Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.





# Finding the difference Arrange two groups so that the difference between the groups can be worked out.

8 is 2 more than 6. 6 is 2 less than 8. The difference between 8 and 6 is 2.

#### Subtraction within 20

Understand when and how to subtract 1s efficiently.

Use a bead string to subtract 1s efficiently.

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5 - 3 = 2 15 - 3 = 12

Subtracting 10s and 1s For example: 18 – 12

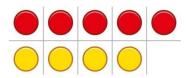
Subtract 12 by first subtracting the 10, then the remaining 2.



First subtract the 10, then take away 2.

#### Finding the difference

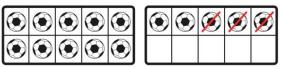
Represent objects using sketches or counters to support finding the difference.



5 - 4 = 1The difference between 5 and 4 is 1.

#### Subtraction within 20

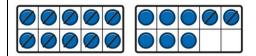
Understand when and how to subtract 1s efficiently.



5 - 3 = 215 - 3 = 12

Subtracting 10s and 1s For example: 18 – 12

Use ten frames to represent the efficient method of subtracting 12.



First subtract the 10, then subtract 2.

#### Finding the difference

Children understand 'find the difference' as subtraction.



10 - 4 = 6The difference between 10 and 6 is 4.

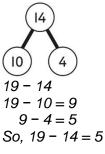
#### Subtraction within 20

Understand how to use knowledge of bonds within 10 to subtract efficiently.

5 - 3 = 2 15 - 3 = 12

#### Subtracting 10s and 1s

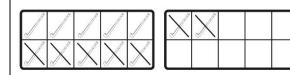
Use a part-whole model to support the calculation.



Subtraction bridging 10 using number bonds For example: 12 – 7

then decide on how to split the 7 into parts.

Arrange objects into a 10 and some 1s,



7 is 2 and 5, so I take away the 2 and then the 5.

#### Year 1 Multiplication

Key Vocab Groups Times Multiply Multiplied by Times-table **Recognising and making equal groups** Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.

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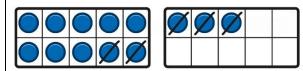
Finding the total of equal groups by counting in 2s, 5s and 10s



There are 5 pens in each pack ... 5...10...15...20...25...30...35...40...

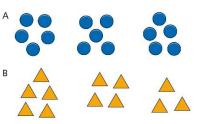
## Subtraction bridging 10 using number bonds

Represent the use of bonds using ten frames.

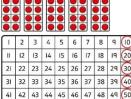


For 13 – 5, I take away 3 to make 10, then take away 2 to make 8.

**Recognising and making equal groups** Children draw and represent equal and unequal groups.

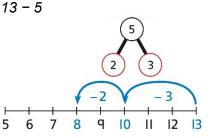


Finding the total of equal groups by counting in 2s, 5s and 10s 100 squares and ten frames support counting in 2s, 5s and 10s.



Subtraction bridging 10 using number bonds

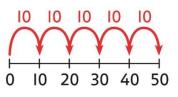
Use a number line and a part-whole model to support the method.



### Describe equal groups using words

*Three equal groups of 4. Four equal groups of 3.* 

Finding the total of equal groups by counting in 2s, 5s and 10s Use a number line to support repeated addition through counting in 2s, 5s and 10s.



Year 1 Division	Grouping Learn to make equal groups from a whole	<b>Grouping</b> Represent a whole and work out how many	<b>Grouping</b> Children may relate this to counting back in
Key Vocab	and find how many equal groups of a certain size can be made.	equal groups.	steps of 2, 5 or 10.
Group Equal groups	Sort a whole set people and objects into	00000 00000	
Divide Share Shared equally	equal groups.	There are 10 in total. There are 5 in each group. There are 2 groups.	0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
	There are 10 children altogether. There are 2 in each group. There are 5 groups.		
	Sharing Share a set of objects into equal parts and work out how many are in each part.	<b>Sharing</b> Sketch or draw to represent sharing into equal parts. This may be related to fractions.	<b>Sharing</b> 10 shared into 2 equal groups gives 5 in each group.

	Year 2		
	Concrete	Pictorial	Abstract
Year 2 Addition			
Understanding 10s and 1s <u>Key Vocab</u> Whole Part Ones Ten Tens Number bond	Group objects into 10s and 1s.	Understand 10s and 1s equipment, and link with visual representations on ten frames.	Represent numbers on a place value grid, using equipment or numerals. Tens Ones 3 2 Tens Ones 4 3
Adding 10s	Use known bonds and unitising to add 10s. ())) ())	Use known bonds and unitising to add 10s. $ \begin{array}{c} \bullet & \bullet \\ \bullet &$	Use known bonds and unitising to add 10s. 7 4 4 + 3 = 4 + 3 = 7 $4 \tan 3 = 7$ $4 \tan $

Adding a 1-digit number to a 2-digit number not bridging a 10 Addition Plus Total Altogether	Add the 1s to find the total. Use known bonds within 10. 10 10 10 10 10 10 10 10 10 10 10 10 10	Add the 1s. + + + + + + + + + + + + + + + + + + +	Add the 1s. Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy. $30 \ 31 \ 32 \ 33 \ 34 \ 35 \ 36 \ 37 \ 38 \ 39 \ 40$ This can be represented horizontally or vertically. 34 + 5 = 39 or $\frac{1}{3} \ \frac{1}{4} \ \frac{5}{9} \ \frac{9}{9}$
Adding a 1-digit number to a 2-digit number bridging 10	Complete a 10 using number bonds.	Complete a 10 using number bonds.	Complete a 10 using number bonds. 7 $5$ $2$ $+5$ $+2$ $+3$ $43$ $44$ $45$ $46$ $47$ $48$ $49$ $50$ $51$ $52$ $53$ $7 = 5 + 2$ $45 + 5 + 2 = 52$

Adding a 1-digit number	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.
to a 2-digit number using exchange			$\begin{array}{c} T \\ \hline 2 \\ + \\ \hline 2 \\ \hline 1 \\ \end{array}$
			T     O       2     4       8       3     2       J
Adding a multiple of 10	Add the 10s and then recombine.	Add the 10s and then recombine.	Add the 10s and then recombine.
to a 2-digit number			37 + 20 = ? 30 + 20 = 50 50 + 7 = 57
	27 is 2 tens and 7 ones. 50 is 5 tens.	\$\$\$\$\$\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$	37 + 20 = 57
	There are 7 tens in total and 7 ones. So, 27 + 50 is 7 tens and 7 ones.	66 is 6 tens and 6 ones. 66 + 10 = 76 A 100 square can support this understanding. 1 2 3 4 5 6 7 8 9 10 1 2 2 3 4 5 6 7 8 9 10 1 2 2 3 4 5 6 7 8 9 10 1 2 2 2 2 2 2 4 2 5 2 7 2 8 2 9 30 3 3 2 2 3 3 4 5 5 6 7 7 8 9 40 4 4 2 4 3 4 4 5 6 6 6 7 6 8 6 70 7 7 7 2 7 3 7 4 7 5 7 6 7 7 8 78 80 8 2 8 3 8 4 8 5 6 6 7 8 8 9 9 100	

Adding a multiple of 10 to a 2-digit number using columns	Add the 10s using a place value grid to support. TOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOO	Add the 10s using a place value grid to support. TO O O O O O O O O O O O O O O O O O O	Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value. $\begin{array}{r} \hline T & O \\ \hline I & 6 \\ + & 3 \\ \hline 4 & 6 \end{array}$ $1 + 3 = 4$ $1 ten + 3 tens = 4 tens$ $16 + 30 = 46$
Adding two 2-digit numbers	Add the 10s and 1s separately. Add the 10s and 1s separately. 5+3=8 There are 8 ones in total. 3+2=5 There are 5 tens in total. 35+23=58	Add the 10s and 1s separately. Use a part-whole model to support. 32 + 11 $11 = 10 + 1$ $32 + 10 = 42$ $42 + 1 = 43$ $32 + 11 = 43$	Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations. $\frac{17}{17} + 10 + 10 + 3 + 2 + \frac{1}{2} - \frac{1}{1} - \frac{1}{7} + \frac{2}{2} - \frac{5}{2} - \frac{1}{2} - \frac{1}{7} - \frac{1}{7} + \frac{1}{2} - \frac{1}{7} - \frac{1}{7$

Adding two 2-digit	Add the 1s. Then add the 10s.	Add the 1s. Then add the 10s.
numbers using a place value grid	Tens Ones + Tens Ones Tens Ones	TO $32$ $+14$ $6$
	+ +	3 2 + 1 4 4 6
Adding two 2-digit	Add the 1s. Exchange 10 ones for a ten. Then add the 10s.	Add the 1s. Exchange 10 ones for a ten. Then add the 10s.
2-digit numbers with exchange	Then add the 10s. Tens Ones 3 6 4 9 9 9 9 9 4 9 9 9 9 9 5 9 9 9 9 5 9 9 9 9 5 9 9 9 9 5 9 5	Then add the 10s. $T \bigcirc 3 6 + 2 9 - 5 - 1 =$

Year 2			
Subtraction			
Subtracting multiples of 10	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.
Key Vocab Subtract Subtraction Find the difference	· · · · · · · · · · · · · · · · · · ·	IOO           30	2 5 20 50
Take away Minus Less	8 subtract 6 is 2. So, 8 tens subtract 6 tens is 2 tens.	10 - 3 = 7 So, 10 tens subtract 3 tens is 7 tens.	7 tens subtract 5 tens is 2 tens. 70 − 50 = 20
Subtracting a single-digit number	Subtract the 1s. This may be done in or out of a place value grid. TO O O O O O O O O O O O O O O O O O	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
Subtracting a single-digit number bridging 10	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.	Bridge 10 by using known bonds. -4 -4 -4 16 17 18 19 20 21 22 23 24 25 26 24 - 6 = ? 24 - 4 - 2 = ?

Subtracting a single-digit number using exchange	Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.	Exchange 1 ten for 10 ones.	Exchange 1 ten for 10 ones. $T \bigcirc 12 \\ 12 \\ 15 \\ - \\ 7 \\ 8 \\ \hline 1 \\ 25 \\ - \\ 7 \\ 1 \\ 8 \\ 25 \\ - \\ 7 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$
Subtracting a 2-digit number	Subtract by taking away.	Subtract the 10s and the 1s. This can be represented on a 100 square. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Subtract the 10s and the 1s. This can be represented on a number line. 7-10 $-10$ $-1$

Subtracting a 2-digit number using place value and columns	Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid. $\begin{array}{c c} T & O \\ \hline & & & \\ \hline \hline & & & \\ \hline & & & \\ \hline \hline & & & \\ \hline \hline & & & \\ \hline \hline \\ \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \hline \hline \\ \hline \hline$	Subtract the 1s. Then subtract the 10s.	Using column subtraction, subtract the 1s. Then subtract the 10s. $\begin{array}{r} T \\ -1 \\ -1 \\ -3 \\ \hline -1 \\ -3 \\ \hline -1 \\ 3 \\ 3 \end{array}$
Subtracting a 2-digit number with exchange		Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s. Tens Ones Ones Ones Ones Ones Ones Ones Ones	Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s. $\frac{T}{4} \frac{O}{5}$ $-\frac{2}{2} \frac{7}{7}$ $\frac{T}{-\frac{O}{3 \# 15}}$ $-\frac{2}{2} \frac{7}{7}$ $\frac{T}{-\frac{O}{3 \# 15}}$ $-\frac{2}{2} \frac{7}{\frac{8}{15}}$ $-\frac{2}{2} \frac{7}{\frac{8}{15}}$ $-\frac{2}{2} \frac{7}{\frac{1}{18}}$

Year 2 Multiplication			
Equal groups and repeated addition	Recognise equal groups and write as repeated addition and as multiplication.	Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.	Use a number line and write as repeated addition and as multiplication.
Key Vocab Groups Times Multiply Multiplied by Times-table	3 groups of 5 chairs 15 chairs altogether	3 groups of 5	$ \begin{array}{c}                                     $
Using arrays to	Understand the relationship between	15 in total Understand the relationship between	Understand the relationship between arrays,
represent multiplication and support understanding	arrays, multiplication and repeated addition.	<ul> <li>arrays, multiplication and repeated addition.</li> <li>arrays, multiplication addition.</li> <li>arrays, multiplication.</li> <li>arrays, multiplication addition.</li> <li>arrays, m</li></ul>	multiplication and repeated addition. $\begin{array}{c} & & \\ & $
Understanding commutativity	Use arrays to visualise commutativity.	Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.	Use arrays to visualise commutativity.
	I can see 6 groups of 3. I can see 3 groups of 6.	This is 2 groups of 6 and also 6 groups of 2.	4 + 4 + 4 + 4 + 4 = 20 5 + 5 + 5 + 5 = 20 $4 \times 5 = 20 \text{ and } 5 \times 4 = 20$

Learning ×2, ×5 and ×10 table facts	Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.	Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.	Understand how the times-tables increase and contain patterns.
		<b>00000000</b>	
	3 groups of 10 10, 20, 30 3 × 10 = 30	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
			$5 \times 10 = 50$ $6 \times 10 = 60$

Year 2 Division			
Sharing equally	Start with a whole and share into equal parts, one at a time.	Represent the objects shared into equal parts using a bar model.	Use a bar model to support understanding of the division.
Key Vocab Group Equal groups Divide Share Shared equally	<ul> <li>Cocococococococococococococococococococ</li></ul>	O shared into 5 equal parts.           There are 4 in each parts.	18 18 ÷ 2 = 9

Grouping equally	Understand how to make equal groups from a whole.	Understand the relationship between grouping and the division statements.	Understand how to relate division by grouping to repeated subtraction.
	<u></u>	$12 \div 3 = 4$	
	8 divided into 4 equal groups. There are 2 in each group.	$12 \div 4 = 3$	0 1 2 3 4 5 6 7 8 9 10 11 12
		12 ÷ 6 = 2	There are 4 groups now.
			12 divided into groups of 3.
		$12 \div 2 = 6$	$12 \div 3 = 4$
			There are 4 groups.
Using known times-tables to solve divisions	Understand the relationship between multiplication facts and division.	Link equal grouping with repeated subtraction and known times-table facts to support division.	Relate times-table knowledge directly to division.
		40 divided by 4 is 10.	$I \times I0 = I0$ $2 \times I0 = 20$ $3 \times I0 = 30$ $4 \times I0 = 40$ $5 \times I0 = 50$ $6 \times I0 = 60$ $7 \times I0 = 70$ $I used the I0$ times-table to help me. $3 \times I0 = 30.$
	<i>4 groups of 5 cars is 20 cars in total.</i> <i>20 divided by 4 is 5.</i>	Use a bar model to support understanding of the link between times-table knowledge and division.	8 × 10 = 80 I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.
		60 []	$3 \times 10 = 30$ so $30 \div 10 = 3$